

## INVESTIGATION INTO THE KINETICS OF AEROSOL FORMATION AT PHOTOLYSIS OF THE TUNGSTEN CARBONYL $W(CO)_6$

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*Kinetics of formation and growth of finely disperse aerosol at tungsten carbonyl photolysis in air is studied experimentally. The emphasis is on the effect of coagulation and the interval between termination of the generation and the time of particle detection ( $t_1$ ) on the measured concentration and the particle size distribution. Kinetics of aerosol formation is numerically simulated within the framework of the Smolukhovskii coagulation model. The rate of generation of condensing products, "monomers"  $F(t)$ , was derived from comparison between the experimental and calculated data. The derived value proves to agree well with the independently measured rate of  $W(CO)_6$  photolysis.*

### 1. INTRODUCTION

Investigation into the processes of disintegration of carbonyls of transient metals remains urgent for the last decades. This is caused by the use of materials based on them in catalysis,<sup>1</sup> radio electronics,<sup>2</sup> etc. Much attention is paid to the study of UV and IR photolysis of carbonyls.<sup>3-5</sup> Products of carbonyl photolysis – atoms or metal oxides (in the presence of oxygen) – can transit into the aerosol state. In this paper, kinetics of photochemical formation of  $W(CO)_6$  aerosol is studied in detail, and dynamics of this process is simulated numerically within the framework of the Smolukhovskii coagulation model. Our main concern was with an increase in reliability and accuracy of the algorithm for calculation of the rate of generation of the condensing molecules ("monomers").

### 2. EXPERIMENT

Kinetics of aerosol formation at  $W(CO)_6$  photolysis was experimentally studied in a through-type system similar to that described earlier in Ref. 6. The air flow, purified with an aerosol filter and a column with a molecular sieve 4A, passed through the thermostatic U-shaped tube at 25°C. The tube contained crystal  $W(CO)_6$  and the air flow became saturated with the carbonyl vapor. The resulting vapor-air mixture came to the Quartz through-type reactor of the laminar type. Vapor of reagents were irradiated with full light of a mercury lamp DRSh-500. Radiation intensity varied by changing the distance from the lamp

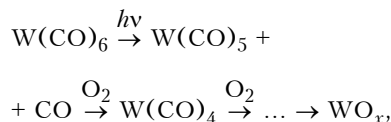
to the reactor. The irradiation time,  $t_0$ , varied within the interval 0.03–15 s with the use of a slit diaphragm set in front of the reactor. The interval between termination of the photolysis and the time of particle detection (the delay time),  $t_1$ , changed from 3.5 to 386 s by setting additional through-type flasks.

The particle number density and size distribution were measured by an automated aerosol spectrometer within the ranges from  $10^2$  to  $10^7$  particle/cm<sup>3</sup> and from 2 to 200 nm size, respectively.

### 3. EXPERIMENTAL RESULTS

#### 3.1. Kinetics of the photochemical aerosol formation

The simplified mechanism of the tungsten carbonyl photolysis in the presence of oxygen can be presented as the following chain of reactions<sup>8</sup>:



where  $x = 2, 3$ . The resulting product is the mixture of  $WO_2$  and  $WO_3$ , just that which forms aerosol particles. Figure 1 presents the aerosol particle number density as a function of the irradiation time.

It should be noted that new monomer molecules are not generated in the interval  $t_1$ . In this time, condensation and coagulation of already formed monomers and clusters take place. As a result, aerosol

particle number density and size distribution are different in the reactor and at the measurement point. Figure 2 presents the experimental dependence of  $N_a$  on  $t_0$  for different values of  $t_1$ .

As seen from the figure, at short  $t_0$  (and small  $N_a$ ) the particle number density increases with increasing  $t_1$ . Conversely, at  $t_0 > 4$  s it decreases with increasing  $t_1$ . That is why the value of  $t_1$  should be taken into account when analyzing the nucleation kinetics for calculation of the rate of monomer generation.

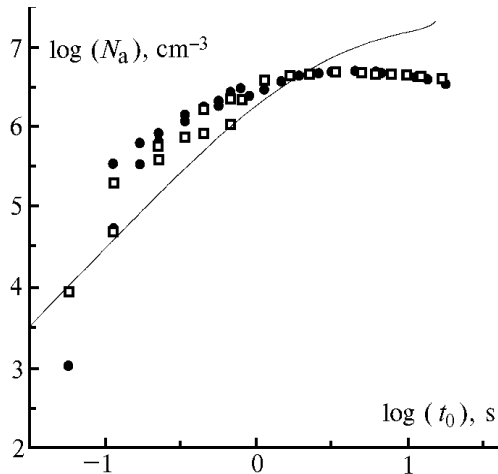


FIG. 1. Particle number density vsx the irradiation time for  $t_1=3.5$  s.  $[W(CO)_6]=1.13 \cdot 10^{13} \text{ cm}^{-3}$ . Experimentally measured  $W_{\text{phot}}=1.69 \cdot 10^9 \text{ cm}^{-3} \cdot \text{s}^{-1}$ , calculated  $F(t)=1.16 \cdot 10^9 \text{ cm}^{-3} \cdot \text{s}^{-1}$ . Dots are for experimental data, the curve is for the calculated results.

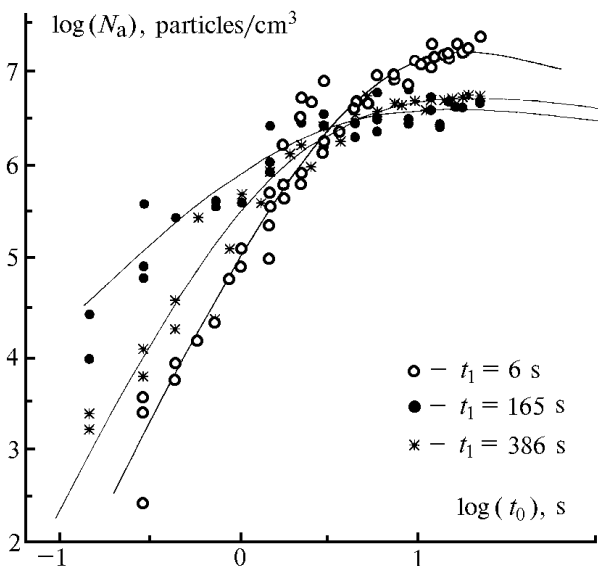


FIG. 2. Particle number density vsx the irradiation time for different values of  $t_1$  and  $W_{\text{rel}}=4 \cdot 10^{-4}$ . Dots are for experimental data, curves are for results of numerical simulation.

### 3.2. Numerical model

In order to find the rate of monomer generation  $F(t)$ , we have calculated numerically the kinetics of aerosol formation within the framework of the Smolukhovskii coagulation model in the mode of free molecular collision of clusters, similar to that described in Ref. 8. Earlier the authors have developed an efficient algorithm for solution of the coagulation equation.<sup>6,9</sup> In this work, the model is modified so that it takes into account the influence of  $t_1$  and aerosol sedimentation on the reactor surface. Similarly to Ref. 8, the main assumptions in this model are as follows:

- 1) the rate of monomer generation  $F(t)$  is constant;
- 2) all collisions of monomers and clusters result in the formation of new clusters;
- 3) there is no evaporation of monomers from the surface of aerosol particles.

In this case, concentration of monomers and clusters varies in time in accordance with the following equations:

$$\frac{dN_1}{dt} = -N_1 \sum_{i=1}^{\infty} \beta_{1i} N_i + F(t) - \gamma_1 N_1, \quad (1)$$

$$\frac{dN_k}{dt} = \frac{1}{2} \sum_{i+j=k} \beta_{ij} N_i N_j - N_k \sum_{i=1}^{\infty} \beta_{ki} N_i - \gamma_k N_k; \quad (2)$$

$F(t) = F = \text{const}$  at  $t \geq \tau_0$ ,  $F(t) = 0$  at  $\tau_0 \leq t \leq \tau_0 + \tau_1$ , where  $N_1$  and  $N_k$  are the concentrations of monomers and clusters consisting of  $k$  monomers;  $\beta_{ij}$  is the gas-kinetic constant of collision of clusters consisting of  $i$  and  $j$  monomers;  $\gamma_i$  is the constant of sedimentation of  $i$ th cluster upon the reactor surface. Following Ref. 8, let us consider the substitution of variables:

$$N_i = k_n n_i \quad t = k_\tau \tau, \quad (3)$$

where  $k_n = (F/\beta_{11})^{1/2}$ ,  $k_\tau = (1/F\beta_{11})^{1/2}$ .

Then, the set of equations (1)–(2) takes the following form:

$$dn_1/d\tau = \tilde{F} - n_1 \sum_{i=1}^{\infty} K_{1i} n_i - \tilde{\gamma}_1 n_1, \quad (4)$$

$$dn_k/d\tau = 1/2 \sum_{i+j=k} K_{ij} n_i n_j - n_k \sum_{i=1}^{\infty} K_{ki} n_k - \tilde{\gamma}_k n_k; \quad (5)$$

$$\tilde{F}(\tau) = 1 \quad \text{at} \quad \tau \leq \tilde{\tau} \leq \tilde{\tau} + \tau_1,$$

$$\tilde{F}(\tau) = 0 \quad \text{at} \quad \tilde{\tau}_0 \leq \tilde{\tau} \leq \tilde{\tau}_0 + \tilde{\tau}_1,$$

where  $\tilde{\tau}_0 = \tau_0/k_\tau$ ,  $\tilde{\tau}_1 = \tau_1/k_\tau$ ,  $\tilde{\gamma}_1 = \gamma_1/k_\tau$ ,  $K_{ij} = \beta_{ij}/\beta_{11}$ . In the case of free molecular collisions,  $K_{ij} = 1/4\sqrt{2} (i^{1/3} + j^{1/3})^2 (1/i + 1/j)^{1/2}$ . (6)

To solve the Cauchy problem presented by Eqs. (4)–(5), the section finite-element algorithm proposed by the authors was applied. This algorithm uses 50 point and 80 cubic finite elements for approximation of the aerosol particle number density spectrum. Experimental data and the calculated curves were compared similarly to the method given in Ref. 6.

Since Eqs. (4)–(5) contain the unknown value  $k_\tau$ , the theoretical kinetic curves were calculated by iterations, but with refinement of the  $k_\tau$  value at each iteration. For given  $k_\tau$ , the values of  $\tilde{\tau}_1$  and  $\tilde{\gamma}_1$  were calculated, and the solution of Eqs. (4)–(5) were found for  $10^{-2} \leq \tau_0 \leq 30$  and calculated  $\tilde{\tau}_1$  and  $\tilde{\gamma}_1$ . Then the temporal dependence  $\tilde{N}_J(\tau_0) = \sum_{l=J}^{\infty} n_l(\tau_0)$  of the total number density of clusters of the size  $l \geq J$  on  $\tau_0$  was found for a given  $J$ . Selecting the same scales on logarithmic scale along the vertical and horizontal axes, we used the parallel transfer of the experimental points ( $\delta_y$  along the  $y$ -axis and  $\delta_x$  along the  $x$ -axis) for those to be maximally close to the calculated curve. The parameters  $\delta_y$  and  $\delta_x$  were found by minimizing the functional:

$$\Phi_J(\delta_y, \delta_x) = \sum_{i=1}^{20} (y_i + \delta_i - \phi(x_i + \delta_x))^2,$$

where  $y_i$  and  $x_i$  are the logarithms of the parameters  $N_J(t)$  and  $t(t)$ ;  $N_J(t) = \sum_{l=J}^{\infty} n_l(t)$  is the experimentally measured total number density of clusters of the size  $l \geq J$ ;  $\phi(x)$  is the value at the point  $x$  of the spline reconstructed from the calculated data  $\tilde{N}_J(\tau_0)$ . Then a new value of  $k_\tau = 10^{\delta_x}$  is calculated.

This procedure started with the initial value  $k_\tau = 1$ . It repeated until  $k_\tau$  coincides with the preceding value accurate to two significant digits. Usually 3–4 iterations were enough; further  $k_\tau$  stopped to refine. The monomer generation rate  $F(t)$  can be estimated as  $F(t) = k_n/k_\tau \approx 10^{\delta_y - \delta_x}$ .

#### 4. DISCUSSION

One of the main problems of numerical modeling of the nucleation kinetics is the calculation of the value of  $F(t)$ . In this paper, the additional parameter  $t_1$  is taken into account in the model.

As noted above, to calculate  $F(t)$ , it is necessary, first, to estimate the minimal detectable value  $J$  from the minimum of the functional  $\Phi_J$ . The Table I gives a number of  $\Phi_J$  values calculated for different  $t_1$  and  $J$  using the experimental data from Fig. 2.

As seen from the Table,  $\Phi_J$  is minimal at  $J = 5$ . This means that detectable are particles consisting of 5

and more monomers. The numerical modeling shows that, if the accuracy of  $J$  determination is  $\pm 1$ , then this results in a  $\pm 30\%$  uncertainty in  $F(t)$  calculation. Besides, the greater  $t_1$  and spread in experimental data, the weaker  $J$  dependence of  $\Phi_J$  and the greater error in the  $F(t)$  determination.

TABLE I. The values of the functional  $\Phi_J \times 0.1$  for different  $t_1$  and  $J$ .

$t_1$	6	40	165	386
$J$	$\Phi_J$	$\Phi_J$	$\Phi_J$	$\Phi_J$
2	0.600	0.381	0.249	0.217
4	0.223	0.130	0.159	0.342
6	0.288	0.194	0.150	0.406
10	0.602	0.386	0.159	0.472

The constant of  $W(\text{CO})_6$  photolysis was measured independently, the rate of photolysis  $W_{\text{phot}}$  was determined for the conditions of the experiment (see Fig. 1). We have found  $W_{\text{phot}} = 1.69 \cdot 10^9 \text{ cm}^{-3} \cdot \text{s}^{-1}$ . The value calculated from the model is  $F(t) = 1.16 \cdot 10^9 \text{ cm}^{-3} \cdot \text{s}^{-1}$ . Thus, the experimentally measured rate of  $W(\text{CO})_6$  photolysis coincides with the rate of monomer generation calculated from the model. If  $F(t)$  is calculated neglecting  $t_1$ , then the resulting value is  $5.41 \cdot 10^8 \text{ cm}^{-3} \cdot \text{s}^{-1}$ . So, the neglect of  $t_1$  in  $F(t)$  calculation results in large errors.

#### CONCLUSIONS

Influence of coagulation and the delay time  $t_1$  on the formation kinetics of aerosol particles of the nanometer size range at tungsten carbonyl photolysis has been studied.

The kinetics of  $W(\text{CO})_6$  aerosol formation has been modeled numerically within the framework of the modified Smolukhovskii coagulation model accounting for the value of  $t_1$ .

The rate  $F(t)$  of generation of the condensing products closely coincides with the independently measured rate of  $W(\text{CO})_6$  photolysis. Thus, it is shown that the account for  $t_1$  increases the reliability of  $F(t)$  reconstruction.

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